

Chapter \Rightarrow 2
Real Numbers.

1 Natural Numbers $\rightarrow 1, 2, 3, \dots$

2 Whole Numbers $\rightarrow 0, 1, 2, 3, 4, 5, \dots$

3. Integer $\rightarrow \underbrace{-3, -2, -1}_{\text{Negative Integer}}, 0, \underbrace{1, 2, 3}_{\text{Positive Integer}}, \dots$

4. Rational Numbers \rightarrow Number which can be represented in $\frac{p}{q}$ form where p and q are integers and where $q \neq 0$
Ex $\rightarrow \frac{1}{4}, \frac{2}{3}$

(i) Terminate after definite decimal expansion
ex $\Rightarrow \frac{1}{4} = 0.25, \frac{2}{16} = 0.125$

(ii) Non Terminate but repeating decimal expansion
ex $\Rightarrow \frac{2}{3} = 0.666, \frac{100}{7} = 14.2857142$

Prime Number \Rightarrow Natural Number greater than one which is not divisible by any number except 1 and itself
ex - 2, 3, 5, 7, 11, 13, 17, 19, 23, 29 etc.

Irrational Number \rightarrow Number which can't be expressed in $\frac{p}{q}$ form where p & q are integer & where $q \neq 0$
Ex $\Rightarrow \sqrt{2}, \sqrt{3}, \sqrt{5}, \sqrt{7}$

Composite No \rightarrow Natural one which is divisible by one other than 1 and itself

Euclid division Lemma \Rightarrow A lemma is previous statement which is used to prove other statement

\rightarrow Euclid division Lemma is a restatement of long division process.

$$\text{Divisor} = b \overline{) a} \begin{array}{l} \text{Divident} \\ \text{quotient} \end{array}$$

r \rightarrow remainder

$$a = bq + r$$

where $0 < r < b$

a, b, q, r integers.

Exercise \Rightarrow 2.1

Q-1 Square of any positive odd integers is of the form $4q+1$, where q is any integer

Ans Let a is any positive integer and $b = 2$
By euclid division lemma there exists integer m and r such that
 $a = 2m + r$ $0 \leq r < 2$

$$a = 2m + r$$

$$(r = 0, 1)$$

By putting = $a = 2m + r$
 $a = 2m + 0$
 $a = 2m$

$$a = 2m + r$$
$$a = 2m + 1$$

$$a = 2m + 1$$

$$a^2 = (2m + 1)^2$$

$$= (a + b)^2 = a^2 + 2ab + b^2$$

$$\Rightarrow 2m^2 + 2 \times 2m \times 1 + 1^2$$

$$\Rightarrow 4m^2 + 4m + 1$$

$$a^2 \Rightarrow 4(m^2 + m) + 1$$

$$a^2 \Rightarrow 4q + 1 \quad (q = m^2 + m)$$

So, a is any positive odd integer and square of it can be written in form of $4q + 1$

Q-2 Use Euclid lemma to show that cube of any positive integer is of the form $9q$ or $9q + 1$ or $9q + 8$ when q is some integer.

Ans Let a is any positive integer, $b = 3$

By Euclid division lemma there exists integer

$$m \text{ and } r \text{ such that } a = 3m + r$$

$$(r = 0, 1, 2)$$

By putting the value.

$$a = 3m + 1$$

$$a = 3m + 0$$

$$a = 3m$$

$$a = 3m + 1$$

$$a = 3m + 1$$

$$a = 3m + 1$$

$$a = 3m + 2$$

Case 1 $a = 3m$

$$(a)^3 = (3m)^3$$

$$(a)^3 = 27m^3$$

$$(a)^3 = 9(3m^3)$$

$$9q \Rightarrow 3m^3$$

$$(a)^3 = 9q$$

Case 2 $a = 3m + 1$

$$(a)^3 = (3m + 1)^3$$

$$= (a)^3 + 3(a)^2(b) + 3(a)(b)^2 + (b)^3$$

$$= (3m)^3 + 3(3m)^2(1) + 3(3m)(1)^2 + (1)^3$$

$$\Rightarrow 27m^3 + 27m^2 + 9m + 1$$

$$(a)^3 \Rightarrow 9(3m^3 + 3m^2 + m) + 1$$

$$9q = (3m^3 + 3m^2 + m)$$

$$= 9q + 1$$

Case 3 $a = 3m + 2$

$$(a)^3 = (3m + 2)^3$$

$$\Rightarrow (a)^3 + 3(a)^2(b) + 3(a)(b)^2 + (b)^3$$

$$= (3m)^3 + 3(3m)^2(2) + 3(3m)(2)^2 + (2)^3$$

$$= 27m^3 + 54m^2 + 36m + 8$$

$$= 9(3m^3 + 6m^2 + 4m) + 8 \quad 9q = (3m^3 + 6m^2 + 4m)$$

$$9q + 8$$

So, a is any positive integer and cube can express in form of $9q$ or $9q + 1$ or $9q + 8$.

Q-3. Show that any positive odd integer is of the form $6q+1$ or $6q+3$ or $6q+5$ where q is positive integers.

Ans Let a is any positive integer and $b=6$
By Euclid division lemma there exists integers q and r such that
 $a = 6q + r$
($r = 0, 1, 2, 3, 4, 5$)

By putting the value.

- $a = 6q + 0$ (even)
- $a = 6q + 1$ (odd)
- $a = 6q + 2$ (even)
- $a = 6q + 3$ (odd)
- $a = 6q + 4$ (even)
- $a = 6q + 5$ (odd)

So, a is any positive integer can express in the form of $6q+1$ or $6q+3$ or $6q+5$.

Q-4 Use Euclid's division algorithm find HCF.

(1) 210, 55
 $210 > 55$

By Euclid's division
 $d \times q + r$

(i) $210 = 55 \times 3 + 45$ ($r \neq 0$)

$$\begin{array}{r} 55 \overline{) 210} \quad 3 \\ -165 \\ \hline \end{array}$$

(ii) $55 = 45 \times 1 + 10$ ($r \neq 0$)

$$\begin{array}{r} 45 \overline{) 55} \quad 1 \\ -45 \\ \hline \end{array}$$

(iii) $45 = 10 \times 4 + 5$ ($r \neq 0$)

$$\begin{array}{r} 10 \overline{) 45} \quad 4 \\ -40 \\ \hline \end{array}$$

(iv) $10 = 5 \times 2 + 0$ ($r = 0$)

$$\begin{array}{r} 5 \overline{) 10} \quad 2 \\ -10 \\ \hline \end{array}$$

HCF = 5 Ans.

(i) 420, 130

$420 > 130$

By Euclid's division

$$\begin{array}{r} 130 \overline{) 420} \quad 3 \\ -390 \\ \hline \end{array}$$

(i) $420 = 130 \times 3 + 30$ ($r \neq 0$)

$$\begin{array}{r} 30 \overline{) 130} \quad 4 \\ -120 \\ \hline \end{array}$$

(ii) $130 = 30 \times 4 + 10$ ($r \neq 0$)

$$\begin{array}{r} 10 \overline{) 30} \quad 3 \\ -30 \\ \hline \end{array}$$

(iii) $30 = 10 \times 3 + 0$ ($r = 0$)

$$\begin{array}{r} 10 \overline{) 30} \quad 3 \\ -30 \\ \hline \end{array}$$

HCF = 10 Ans.

(iii) 243, 75

$243 > 75$

By Euclid's division

$$\begin{array}{r} 75 \overline{) 243} \quad 3 \\ -225 \\ \hline \end{array}$$

(i) $243 = 75 \times 3 + 18$ ($r \neq 0$)

$$\begin{array}{r} 18 \overline{) 75} \quad 4 \\ -72 \\ \hline \end{array}$$

$75 = 18 \times 4 + 3$ ($r \neq 0$)

$$\begin{array}{r} 3 \overline{) 18} \quad 6 \\ -18 \\ \hline \end{array}$$

$18 = 3 \times 6 + 0$ ($r = 0$)

$$\begin{array}{r} 3 \overline{) 18} \quad 6 \\ -18 \\ \hline \end{array}$$

H.C.F = 3 Ans.

(iv) 135, 225

Ans $225 > 135$

By Euclid's division -

(i) $225 = 135 \times 1 + 90$ ($r \neq 0$)

(ii) $135 = 90 \times 1 + 45$ ($r \neq 0$)

(iii) $90 = 45 \times 2 + 0$ ($r = 0$)

H.C.F = 45 Ans

$$\begin{array}{r} 135 \overline{) 225} \quad 1 \\ \underline{-135} \end{array}$$

$$\begin{array}{r} 90 \overline{) 135} \quad 1 \\ \underline{-90} \end{array}$$

$$\begin{array}{r} 45 \overline{) 90} \quad 2 \\ \underline{-90} \\ 0 \end{array}$$

(v) 38220, 196

$38220 > 196$

By Euclid's division

(i) $38220 = 196 \times 195 + 0$ ($r = 0$)

196 HCF

$$\begin{array}{r} 196 \overline{) 38220} \quad 195 \\ \underline{-38220} \\ 0 \end{array}$$

(vi) 867, 255

$867 > 255$

By Euclid's division

(i) $867 = 255 \times 3 + 102$ ($r \neq 0$)

(ii) $255 = 102 \times 2 + 51$ ($r \neq 0$)

(iii) $102 = 51 \times 2 + 0$ ($r = 0$)

HCF = 51 Ans.

$$\begin{array}{r} 255 \overline{) 867} \quad 3 \\ \underline{-765} \end{array}$$

$$\begin{array}{r} 102 \overline{) 255} \quad 2 \\ \underline{204} \end{array}$$

$$\begin{array}{r} 51 \overline{) 102} \quad 2 \\ \underline{-102} \\ 0 \end{array}$$

Q. 5) If HCF of number 408 and 10392 is expressed in the form of $408x + 10392y$, find x .

$x = 408 \times 5$, find x .

Ans $1032 = 408$.

By Euclid's division

(i) $1032 = 408 \times 2 + 216$ ($x \neq 0$)

(ii) $408 = 216 \times 1 + 192$ ($x \neq 0$)

(iii) $216 = 192 \times 1 + 24$ ($x \neq 0$)

(iv) $192 = 24 \times 8 + 0$ ($x = 0$)

HCF = 24

$$\begin{array}{r} 408 \overline{) 1032} \quad 2 \\ \underline{- 816} \\ 216 \end{array}$$

$$\underline{- 816}$$

$$\begin{array}{r} 216 \overline{) 408} \quad 1 \\ \underline{- 216} \\ 192 \end{array}$$

$$\underline{- 216}$$

$$\begin{array}{r} 192 \overline{) 216} \quad 1 \\ \underline{- 192} \\ 24 \end{array}$$

$$\underline{- 192}$$

$$\begin{array}{r} 24 \overline{) 192} \quad 8 \\ \underline{- 192} \\ 0 \end{array}$$

$$\underline{- 192}$$

$$\underline{0}$$

$$1032x - 408 \times 5 = 24$$

$$1032x - 2040 = 24$$

$$1032x = 24 + 2040$$

$$1032x = 2064$$

$$x = \frac{2064}{1032} = 2 \text{ Ans}$$

Exercise $\Rightarrow 2 \cdot 2 \cdot 2$

Fundamental Theorem of Arithmetic

Every integer is either a prime number or (if composite number) can be represented as the product of prime numbers and this representation is unique, except for order.

Ex 420

$$\begin{array}{r|l} 2 & 420 \\ \hline 2 & 210 \\ \hline 3 & 105 \\ \hline 3 & 35 \\ \hline 5 & 7 \\ \hline & 1 \end{array}$$

Q-1 Express in form of prime factors.

(i) 468

$$\begin{array}{r|l} 2 & 468 \\ \hline 2 & 234 \\ \hline 3 & 117 \\ \hline 3 & 39 \\ \hline 13 & 13 \\ \hline & 1 \end{array}$$

$$468 \Rightarrow 2 \times 2 \times 3 \times 3 \times 13$$

$$468 \Rightarrow 2^2 \times 3^2 \times 13$$

(ii) 140

$$\begin{array}{r|l} 2 & 140 \\ \hline 2 & 70 \\ \hline 5 & 35 \\ \hline 7 & 7 \\ \hline & 1 \end{array}$$

$$140 \Rightarrow 2 \times 2 \times 5 \times 7$$

$$140 \Rightarrow 2^2 \times 5 \times 7$$

(iii) 945

3	945
3	315
3	105
5	35
7	7
	1

$$945 = 3 \times 3 \times 3 \times 5 \times 7$$

$$3^3 \times 5 \times 7$$

(iv) 3825

3	3825
3	1275
3	425
5	85
17	17
	1

$$3825 = 3 \times 3 \times 3 \times 5 \times 17$$

$$= 3^3 \times 5^2 \times 17$$

(v) 20570

2	20570
5	10285
11	2057
11	187
17	17
	1

$$20570 = 2 \times 5 \times 11 \times 11 \times 17$$

$$= 2 \times 5 \times 11^2 \times 17$$

Q-2 Find the LCM and HCF of the following numbers and verify the $HCF \times LCM = \text{product of the numbers}$.

Relation $HCF(a,b) \times LCM(a,b) = a \times b$

(i) 96, 404

2	96
2	48
2	24
2	12
2	6
3	3
	1

2	404
2	202
101	101
	1

2	96, 404
2	48, 202
2	24, 101
2	12, 101
2	6, 101
3	3, 101
101	1, 101
	1, 1

Sol.

$$96 \Rightarrow 2 \times 2 \times 2 \times 2 \times 2 \times 3 \Rightarrow 2^5 \times 3$$

$$404 \Rightarrow 2 \times 2 \times 101 \Rightarrow 2^2 \times 101$$

$$\text{HCF} \Rightarrow 2 \times 2 = 4$$

$$\text{LCM} = 2^5 \times 3 \times 101 \Rightarrow 9696$$

$$\text{HCF} \times \text{LCM} \Rightarrow 96 \times 404$$

$$4 \times 9696 = 38784 \Rightarrow 38784 \text{ Ans}$$

ii) 336, 54.

<u>Sol.</u>	2 336	2 54	or	2 336, 54
	2 168	3 27		2 168, 27
	2 84	3 9		2 84, 27
	2 42	3 3		3 42, 27
	3 21	1		3 21, 27
	7 7			3 7, 9
	1			3 7, 3
				7 7, 1
				1 1

$$336 \Rightarrow 2 \times 2 \times 2 \times 3 \times 7 = 2^4 \times 3 \times 7$$

$$54 \Rightarrow 2 \times 3 \times 3 \times 3 = 2 \times 3^3$$

$$\text{HCF} = 2 \times 3 = 6, \text{LCM} = 2^4 \times 3^3 \times 7$$

$$\text{HCF} \times \text{LCM} = 336 \times 54$$

$$6 \times 3024 = 18144$$

$$18,144$$

iii) 90, 144

2	90	2	144	Or	2	90, 144
3	45	2	72		2	45, 72
3	15	2	36		2	45, 36
5	5	2	18		2	45, 18
	1	3	9		3	45, 9
		3	3		3	15, 3
			1		5	5, 1
						1, 1

$$90 = 2 \times 3 \times 3 \times 5 \Rightarrow 2 \times 3^2 \times 5$$

$$144 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \Rightarrow 2^4 \times 3^2$$

$$HCF = 2 \times 3 \times 3 \Rightarrow 18$$

$$LCM = 2^4 \times 3^2 \times 5 = 720$$

$$HCF \times LCM$$

$$18 \times 720 = 90 \times 144$$

$$\Rightarrow 12960 = 12960.$$

Q-3. Find the LCM and HCF of the following integers by applying the Prime factorisation method

(i) 12, 15 and 21.

Ans.

2		12
2		6
3		3
		1

3		15
5		5
		1

3		21
7		7
		1

$$12 = 2 \times 2 \times \textcircled{3} \quad | \quad 2^2 \times 3$$

$$15 = \textcircled{3} \times 5$$

$$21 = \textcircled{3} \times 7$$

$$\text{HCF} \Rightarrow 3$$

$$\text{LCM} \Rightarrow 2^2 \times 3 \times 5 \times 7 \Rightarrow 420$$

(b) 24, 15, 36

Ans.

2		24
2		12
2		6
3		3
		1

3		15
5		5
		1

2		36
2		18
3		9
3		3
		1

$$24 \Rightarrow 2 \times 2 \times 2 \times \textcircled{3} \quad | \quad 2^3 \times 3$$

$$15 \Rightarrow \textcircled{3} \times 5$$

$$36 \Rightarrow 2 \times 2 \times \textcircled{3} \times 3 \quad | \quad 2^2 \times 3^2$$

$$\text{HCF} \Rightarrow 3$$

$$\text{LCM} \Rightarrow 2^3 \times 3^2 \times 5 = 360$$

1c) 17, 23, 29.

Ans

17		17
		1
<hr/>		

23		23
		1
<hr/>		

29		29
		1
<hr/>		

$17 \Rightarrow 17 \times 1$

$23 \Rightarrow 23 \times 1$

$29 \Rightarrow 29 \times 1$

$HCF \Rightarrow 1$

$LCM \Rightarrow 17 \times 23 \times 29$

$\Rightarrow 11339.$

1d) 6, 72, 120

Ans

2		6
3		3
		1
<hr/>		

2		72
2		36
2		18
3		9
3		3
		1
<hr/>		

2		120
2		60
2		30
3		15
5		5
		1
<hr/>		

$6 \Rightarrow 2 \times 3$

$72 \Rightarrow 2 \times 2 \times 2 \times 3 \times 3$

$120 \Rightarrow 2 \times 2 \times 2 \times 3 \times 5$

$HCF \Rightarrow 2 \times 3 = 6$

$LCM = 2^3 \times 3^2 \times 5$

$= 360$

(e) 40, 36 and 126

2	40	2	36	2	126
2	20	2	18	3	63
2	10	3	9	3	21
5	5	3	3	7	7
	1		1		1

$40 = 2 \times 2 \times 2 \times 5 = 2^3 \times 5$
 $36 = 2 \times 2 \times 3 \times 3 = 2^2 \times 3^2$
 $126 = 2 \times 3 \times 3 \times 7 = 2 \times 3^2 \times 7$
 $HCF = 2$
 $LCM = 2^3 \times 3^2 \times 5 \times 7 = 2520 \text{ Ans.}$

(4) 8, 9 and 25.

2	8	3	9	5	25
2	4	3	3	5	5
2	2		1		1
	1				

$8 = 2 \times 2 \times 2 = 2^3 \times 1$
 $9 = 3 \times 3 = 3^2 \times 1$
 $25 = 5 \times 5 = 5^2 \times 1$
 $HCF = 1$
 $LCM = 2^3 \times 3^2 \times 5^2$

Q-4 There is circular path around a sports field. Raman takes 40 min to complete one round of the circular path while Anupriya takes 12 min for the same suppose

both of them start from the same point and at the same time and go in the same direction. After how many min. will they meet against the starting point.

2	18
3	9
3	3
	1

2	12
2	6
3	3
	1

$$18 = 2 \times 3 \times 3 = 12 \times 3^2$$

$$12 = 2 \times 2 \times 3 = 2^2 \times 3$$

$$LCM = 2^2 \times 3^2 = 4 \times 9 = 36 \text{ Min}$$

Q-5 In a seminar number of participants in Hindi and Eng and Math are 60, 84, and 108. If equal no. of participants of same subject are sitting in each room then find the best no. of room required.

2	60
2	30
3	15
5	5
	1

2	84
2	42
3	21
7	7
	1

2	108
2	54
2	27
3	9
3	3
	1

$$60 = 2^2 \times 3 \times 5$$

$$84 = 2^2 \times 3 \times 7$$

$$108 = 2 \times 2 \times 3^3$$

$$HCF = 2^2 \times 3 = 12$$

$$\text{Required room} = \frac{\text{Total Participants}}{\text{Participants in one room (H.C.F.)}}$$

$$= \frac{60 + 34 + 108}{12}$$

$$= \frac{202}{12} = 16.83$$

Exercise \Rightarrow 2.3

Theorem (2.3) \rightarrow Let 'P' is a prime and 'a' is positive integer, if 'P' divides a^2 then P also divide 'a'

Ex \rightarrow 2 divides 36 (6^2) then 2 also divides '6'

Co-prime \rightarrow Two positive integers are known as Co-prime if they have only one common factor i.e. 1.
Ex - (2, 3)

Proof by Irrationality

Proof by Contradiction

We want to prove 'J' statement

- (i) We assume 'not y'
- (ii) Find contradiction
- (iii) Claim 'not y' is false it
- (iv) means 'y' statement true.

Q-1 Prove that $5 - \sqrt{3}$ is irrational

Sol: Suppose $5 - \sqrt{3}$ is rational number then $5 - \sqrt{3}$ can be expressed as $5 - \sqrt{3} = \frac{p}{q}$ (where p and q are coprime, $q \neq 0$)

$$5 - \sqrt{3} = \frac{p}{q}$$

$$\frac{5 - p}{q} = \sqrt{3}$$

$$5 - p = \sqrt{3}q$$

Since 5, p, q are integers, so $\frac{5-p}{q}$ is a rational number. Because it is equal to $\sqrt{3}$. So $\sqrt{3}$ is rational but this contradicts the fact that $\sqrt{3}$ is irrational number. So our hypothesis is wrong so we can conclude that $\sqrt{3}$ is irrational number.

Q-2. Prove that $\frac{1}{\sqrt{2}}$ is irrational.

Sol. Suppose $\frac{1}{\sqrt{2}}$ is a rational number then $\frac{1}{\sqrt{2}}$ can be expressed as $\frac{p}{q}$ where p and q are co-prime and q $\neq 0$.

$$\frac{1}{\sqrt{2}} = \frac{p}{q}$$

$$\sqrt{2} = \frac{q}{p}$$

Since 2, p, q are integers, so $\frac{q}{p}$ is a rational number.

Because it is equal to $\sqrt{2}$. So $\sqrt{2}$ is rational number. but this contradicts the fact that $\sqrt{2}$ is irrational number. So our hypothesis is wrong. So we can conclude that $\frac{1}{\sqrt{2}}$ is irrational number.

(ii) $6 + \sqrt{2}$.

Sol Suppose $6 + \sqrt{2}$ is a rational number then $6 + \sqrt{2}$ can be expressed as $\frac{6 + \sqrt{2}}{1} = \frac{P}{Q}$ (where P and Q are \mathbb{Z} -numbers and $Q \neq 0$)

$$\sqrt{2} = \frac{P - 6}{Q}$$

$$\sqrt{2} = \frac{P - 6Q}{Q}$$

Since $6, P, Q$ are integers, so $\frac{P - 6Q}{Q}$ is rational no.

Because it is equal to $\sqrt{2}$, so $\sqrt{2}$ is rational no. but this contradicts the fact $\sqrt{2}$ is irrational no. so our hypothesis is wrong. so we can conclude that $6 + \sqrt{2}$ is irrational no.

(ii) $3\sqrt{2}$ Ans Let us assume the contrary that $3\sqrt{2}$ is Rational

$$3\sqrt{2} = \frac{p}{q} \quad (p \text{ and } q, \text{ are co-prime})$$

$$\sqrt{2} = \frac{p}{3q}$$

$\frac{p}{3q}$ is in the form of $\frac{p}{q}$ then it is Rational.

But we know that $\sqrt{2}$ is Irrational

So, the Contradiction is arisen because of our incorrect assumption.

Q-3. Prove that $\sqrt{p} + \sqrt{q}$ is irrational

Sol. Suppose $\sqrt{p} + \sqrt{q}$ is rational number then can be expressed as \rightarrow

$$\sqrt{p} + \sqrt{q} = \frac{a}{b} \quad (\text{where } a, b \text{ are co-prime}) \\ (b \neq 0)$$

$$\sqrt{p} + \sqrt{q} = \frac{a}{b}$$

$$\therefore \sqrt{q} = \frac{a}{b} - \sqrt{p}$$

both side square

$$(\sqrt{q})^2 = \left(\frac{a}{b} - \sqrt{p}\right)^2$$

$$q = \left(\frac{a}{b}\right)^2 - 2\left(\frac{a}{b}\right)(\sqrt{p}) + (p)$$

$$q = \frac{a^2}{b^2} - 2\frac{a}{b}\sqrt{p} + p$$

$$2\frac{a}{b}\sqrt{p} \Rightarrow \frac{a^2}{b^2} + \frac{p}{1} - q$$

$$2\frac{a}{b}\sqrt{p} \Rightarrow \frac{a^2 + b^2(p-q)}{b^2} \quad [\sqrt{p} + \sqrt{q} \text{ is irrational}]$$

$$\sqrt{p} \Rightarrow \frac{a^2 + b^2(p-q)}{2ab}$$

a, b, p, q are integer $\frac{a^2 + b^2(p-q)}{2ab}$ is rational.

number. Because it is equal to \sqrt{p} so \sqrt{p} is a rational number. But it contradicts the fact that \sqrt{p} is irrational number so our hypothesis is wrong.

(iv) $\frac{17}{6} \Rightarrow \frac{17}{2 \times 3} \Rightarrow$ Denominator 2×3 of $\frac{17}{6}$ is in not in form of $2^m \times 5^n$: so Non-terminating decimal expansion

(v) $\frac{129}{2^2 \times 5^2 \times 7} \Rightarrow$ Denominator $2^2 \times 5^2 \times 7$ of $\frac{129}{2^2 \times 5^2 \times 7}$ is in not in form of $2^m \times 5^n$: so Non-terminating decimal expansion

(vi) $\frac{35}{50} \Rightarrow \frac{35}{2^1 \times 5^2} \Rightarrow$ Denominator $2^1 \times 5^2$ of $\frac{35}{50}$ is in form of $2^m \times 5^n$: so-terminating decimal expansion

(vii) $\frac{7}{80} \Rightarrow \frac{7}{2^4 \times 5} \Rightarrow$ Denominator $2^4 \times 5$ of $\frac{7}{80}$ is in form of $2^m \times 5^n$ so Terminating decimal expansion

Q-2 Write down the decimal expansion of those rational numbers

(i) $\frac{13}{125} \Rightarrow \frac{13}{5 \times 5 \times 5} = \frac{13}{5^3 \times 2^0} \Rightarrow$ Denominator 125 is in form of $2^m \times 5^n$ so terminating decimal expansion

$$\frac{13}{5^3} \times \frac{2^3}{2^3} = \frac{13 \times 8}{(5 \times 2)^3} = \frac{104}{1000} \Rightarrow 0.104$$

(ii) $\frac{1458}{625} \Rightarrow \frac{14588}{5 \times 5 \times 5 \times 5} = \frac{14588}{5^4 \times 2^0} \Rightarrow$ Denominator 625 is in form of $2^m \times 5^n$. so terminating decimal expansion

$$\frac{14588}{5^4} \times \frac{2^4}{2^4} \Rightarrow \frac{14588 \times 16}{(10)^4} = \frac{233408}{10000} \Rightarrow 23.3408$$

(iii) $\frac{49}{800} \Rightarrow \frac{49}{2^2 \times 5^3} \Rightarrow$ Denominator 800 is in form of $2^m \times 5^n$ so. Terminating decimal expansion

$$\frac{49 \times 2^1}{2^2 \times 5^3} \Rightarrow \frac{49 \times 2}{10^3} = \frac{98}{1000} = 0.098$$

Q-3 Decide whether they are rational or not: If rational write the note on prime factors of its denominator

(i) $0.120120012000.120000 \Rightarrow$ Decimal expansion is non-terminating and non-repeating is it irrational number

(ii) 43.123456789

$\frac{43123456789}{10^9} \Rightarrow \frac{43123456789}{2^9 \times 5^9} \Rightarrow$ Denominator is $2^9 \times 5^9$ Prime factors contain in 2 and 5.

It is in form of $2^m \times 5^n$ so it is Rational number with terminating expansion.